

Outline for Day 15

Office hours: 1 - 2
3 - 3:45In which we learn about the atom using the ψ_{210} solution.

- Visualizing the probability density
- What fraction of the time does the electron spend within a_B of the nucleus?
- What is the most likely value of r for the electron?
- What is the average value of r for the electron?
- Spectroscopy of atoms

Outline for Day 15

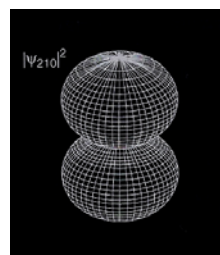
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$$|\psi_{210}|^2 = A \left(\frac{r}{a}\right)^2 e^{-r/a} \cos^2 \theta$$



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Radial Probability Density

$$P(r, \theta, \varphi) = |\psi_{nlm}|^2 dV = |\psi_{nlm}|^2 r^2 \sin\theta dr d\theta d\varphi$$

$$P(r) = B(\theta, \varphi) |R_{nl}|^2 r^2$$

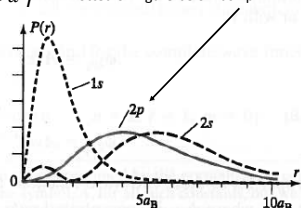
$$|\psi_{210}|^2 = A \left(\frac{r}{a}\right)^2 e^{-r/a} \cos^2\theta$$

$$P_{210}(r) = B(\theta) \left(\frac{r}{a}\right)^2 e^{-r/a} r^2$$

Plotted on figure below as 2p

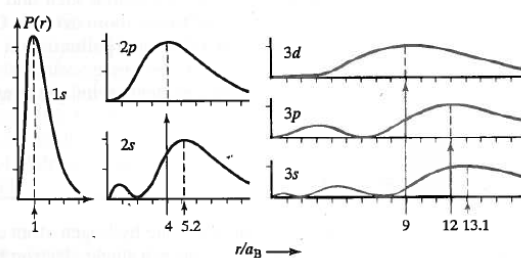
FIGURE 8.22

The radial probability density for the 2p states (solid curve). The most probable radius is $r = 4a_B$. For comparison, the dashed curves show the 1s and 2s distributions to the same scale.

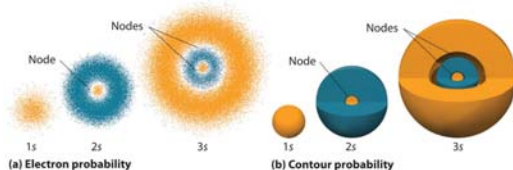


Radial Probability Density

$$P(r) = B(\theta, \varphi) |R_{nl}|^2 r^2$$

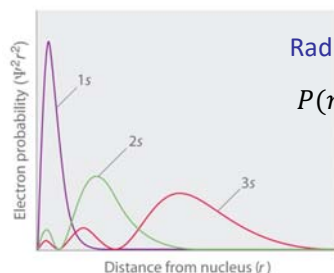


most probable radius indicated for each state



Radial Probability Density

$$P(r) = B(\theta, \varphi) |R_{nl}|^2 r^2$$



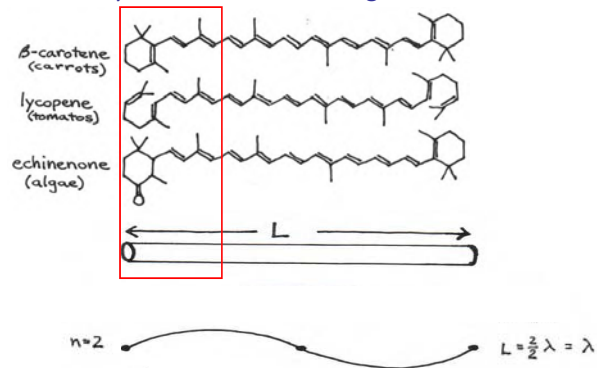
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Probability to find electron in region inside red box?



What is the probability of finding particles between 0 and $\frac{a}{4}$

$$P_{0 \rightarrow \frac{a}{4}} = \int_0^{\frac{a}{4}} \frac{2}{a} \sin^2\left(\frac{n\pi x}{a}\right) dx \quad n = \text{integer}$$

for $n = 2$ state

$$P_{0 \rightarrow \frac{a}{4}} = \frac{2}{a} \int_0^{\frac{a}{4}} \sin^2\left(\frac{2\pi x}{a}\right) dx$$

$$= \frac{2}{a} \left[\frac{x}{2} - \frac{a \sin\left(\frac{4\pi x}{a}\right)}{8\pi} \right]_0^{\frac{a}{4}}$$

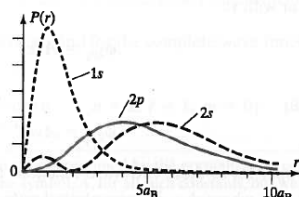
$$= \frac{2}{a} \left[\frac{a}{8} - \frac{a \sin\pi}{8\pi} - 0 - 0 \right]$$

$$= \frac{1}{4}$$

Probability to find electron in 2p state inside Bohr radius in hydrogen atom?

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The radial probability density for the 2p states (solid curve). The most probable radius is $r = 4a_B$. For comparison, the dashed curves show the 1s and 2s distributions to the same scale.



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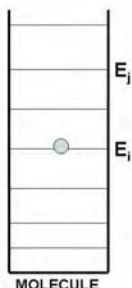
Absorption of Photons

Energy spacing given by:

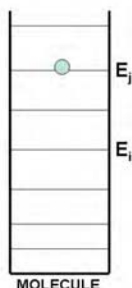
$$E_n = \frac{n^2 \pi^2 \hbar^2}{2ma^2}$$

$$E_{\text{photon}} = E_j - E_i$$

PHOTON



BEFORE ABSORPTION



AFTER ABSORPTION

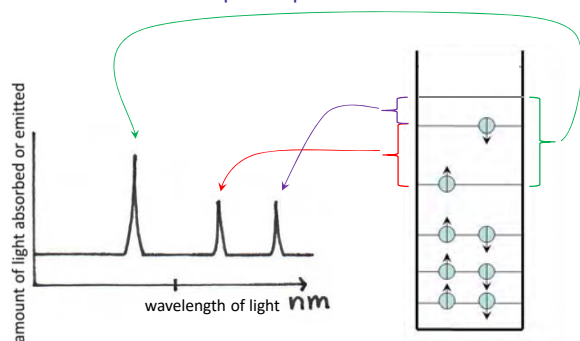
What is the wavelength of a photon that can excite a particle from the m to n state? $n > m$

$$\Delta E_{nm} = E_n - E_m = (n^2 - m^2) \left(\frac{\pi^2 \hbar^2}{2ma^2} \right)$$

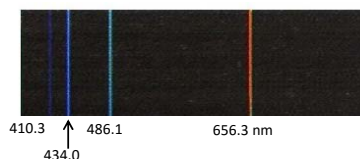
$$\Delta E_{nm} = hf_{nm} = \frac{hc}{\lambda_{nm}}$$

$$\lambda_{nm} = \frac{8\pi^2 ma^2}{h(n^2 - m^2)}$$

Absorption Spectrum



Balmer series: A closer look at the spectrum of hydrogen



Balmer (1885) noticed wavelengths followed a progression

$$\lambda = \frac{91.19 \text{ nm}}{\frac{1}{2^2} - \frac{1}{n^2}} \quad \text{where } n = 3, 4, 5, 6, \dots$$

Balmer used this formula to predict additional lines in the hydrogen spectrum.

How Rydberg equation and Bohr Atom fit together

Balmer-Rydberg Formula

$$\lambda = \frac{91.19\text{nm}}{\frac{1}{m^2} - \frac{1}{n^2}}$$

Predicts λ of $n \rightarrow m$ transition: